

Table A1. Variables and constants used for modeling the *lac* operon.

Parameter	Definition	Value
$L_{(e)}$	External lactose concentration	
X	External IPTG or TMG	
L	Internal lactose concentration	
A	Allolactose concentration	
R	Active (=DNA binding) LacI concentration	
Z	LacZ concentration	
Y	LacY concentration	
$\beta_{y,z}(L)$	The regulation function expressing the production rate of LacZ (or LacY) as a function of external lactose (or IPTG) concentration L	
R_T	Total amount of repressor (constant)	$0.01 \mu\text{M}$ (10 molecules) [10]
Z_T	Maximal amount of LacZ	$50 \mu\text{M}$ ($\sim 10^4$ molecules) [10]
Y_T	maximal amount of LacY	$50 \mu\text{M}$ ($\sim 10^4$ molecules) [10]
$\tau_{\text{cell-generation}}$	Cell generation	30 minutes [17]
$\alpha, \tau_{\text{dilution}}$	Dilution rate	$\frac{\ln 2}{\tau_{\text{cell-generation}}} = 2.26 \times 10^{-2} \text{ min}^{-1} \approx \frac{1}{(50 \text{ min})}$
$\beta_z (\beta_{\text{WT}}, \beta_{\text{max}})$	Maximal production rate of LacZ	$\sim 10^2 \text{ molecules min}^{-1}$ [16]
$\beta_y (\beta_{\text{WT}}, \beta_{\text{max}})$	Maximal production rate of LacY	$\sim 10^2 \text{ molecules min}^{-1}$ [16]
$K_{\text{TMG-y}}$	Affinity of TMG and LacY	$700 \mu\text{M}$ [53]
$K_{L(e)-y}$	Affinity of external lactose and LacY	$400 \mu\text{M}$ [5]
K_{L-y}	Affinity of (internal) lactose and LacY	1.8 mM [5]
K_{L-Z}	Affinity of (internal) lactose and LacZ	1.4 mM [5]
K_{A-Z}	Affinity of Allolactose and LacZ	1.9 mM [17]
K_{A-R}	Affinity of Allolactose and LacI	$6 \mu\text{M}$ [17]
$K_{\text{IPTG-R}}$	Affinity of IPTG and LacI	Assumed to be $1 \mu\text{M}$
$K_{\text{TMG-R}}$	Affinity of TMG and LacI	Assumed to be $6.3 \mu\text{M}$
$K_{R-\text{DNA}}$	Affinity of LacI and the DNA	$10^{-10}-10^{-11} \text{ M}$ [53]
v_y	Velocity of pumping by LacY	$3000 \text{ molecules min}^{-1}$ [17]
\bar{v}_y	Velocity of efflux by LacY	$v_y/100$ [5]
v_{z1}	Velocity of internal lactose hydrolysis by LacZ	$v_{z1} = 0.9v_y$ [5]
v_{z2}	Velocity of conversion of lactose to allolactose by LacZ	$20000 \text{ molecules min}^{-1}$ [17]
v_{z3}	Velocity of allolactose hydrolysis by LacZ	$20000 \text{ molecules min}^{-1}$ [17]

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